

# Type-Directed Elaboration of Quasiquotations

## A High-Level Syntax for Low-Level Reflection

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### Abstract

Idris’s reflection features allow Idris metaprograms to manipulate a representation of Idris’s core language as a datatype, but these reflected terms were designed for ease of type checking and are therefore exceedingly verbose and tedious to work with. A simpler notation would make these programs both easier to read and easier to write. We describe a variation of quasiquotation that uses the language’s compiler to translate high-level programs with holes into their corresponding reflected representation, both in pattern-matching and expression contexts. This provides a notation for reflected language that matches the notation used to write programs, allowing readable metaprograms.

**Categories and Subject Descriptors** CR-number [subcategory]: third-level

**Keywords** quasiquotation; proof automation; metaprogramming

### 1. Introduction

Idris [3] is a programming language with dependent types in the tradition of Agda [16] and Cayenne [1]. An important design goal for the Idris team is to enable the construction of embedded languages that can make strong guarantees about the safety of the programs written in them, rather than requiring users of these embedded languages to write proofs themselves. If this goal is to succeed, Idris will require good tools that library authors can use to automate the construction of proofs.

One such tool is *reflection*, in which an Idris program can construct a proof object by inspecting the AST of a the goal type and generating an AST for the proof term. This allows developers of proof automation to write functions that might otherwise be difficult, because eliminating types through pattern matching is unsound.

Idris has a well-defined core language, called TT, and all constructions in the high-level Idris language are given their semantics by defining their translation to TT. This translation process is referred to as *elaboration*. Terms in TT are exceedingly verbose: every binder has a fully explicit type annotation, every name is fully-qualified, and there are no implicit arguments. This verbosity drastically simplifies type checking. The intention is that one need only

trust this simple type checker to be able to trust the rest of the system.

Because Idris reflection works directly with TT terms, it can quickly become overwhelming. Furthermore, the correspondence between high-level Idris terms and their corresponding TT terms are not always obvious to non-expert users of the language. What appears to be a simple function application at the level of Idris code might turn out to have very complicated type-level structure or non-trivial implicit arguments. In the normal course of programming, it is good to hide this complexity and allow the user to focus on her or his programming task, rather than being overwhelmed by minutiae. However, when writing metaprograms using reflection, this becomes an unfortunate trade-off, because the core language can be difficult to connect to user-visible terms. This difficulty is especially unpleasant when using Idris’s *error reflection* [5], in which Idris code can be used to rewrite the compiler’s error messages before they are presented to the user. In fact, it was practical experience with error reflection that motivated the work described in this paper.

We augment the high-level Idris language with *quasiquotations*, in which the Idris elaborator is invoked to transform high-level Idris into *reflected* TT terms using the same translation that produces TT terms for the type checker. Within quasiquoted terms, *antiquotations* allow other reflected terms to be spliced into the quotation. In a pattern context, antiquotations become patterns to be matched by the reflected term at the corresponding position. These quasiquotations allow the best of both worlds: high-level syntax for the uninteresting parts, with details filled in by type-directed elaboration, along with control over the details of term construction when and if it matters.

### Contribution

The contributions of this paper are:

- a novel adaptation of quasiquotations to the context of dependently-typed programming with reflection that allows the use of high-level language syntax to construct and manipulate the corresponding terms in a core language;
- a description of an implementation technique for these quasiquotations in Idris, as an extension of the type-driven elaboration described in Brady’s 2013 paper [3]; and
- demonstrations of the utility of these quasiquotations for proof automation and error message rewriting.

Furthermore, this paper can serve as a demonstration of how to extend a tactic-based elaborator to support a new high-level language feature.

## 2. Related Work

### 2.1 A Brief History of Quasiquoteation

The notion of quasiquoteation was invented by Quine in his 1940 book *Mathematical Logic* [12, pp. 33–37]. While ordinary quoteations allow one to *mention* a phrase rather than *using* it, quasiquoteations allow these quoted expressions to contain variables that stand for other expressions, just as mathematical expressions can contain variables that stand for values. In other words, a specific class of subexpression is treated as a use within a context that is mentioned. Quine used Greek letters to represent variables in quasiquoteations.

The paradigmatic instance of quasiquoteation in programming languages is that found in the Lisp family. Bawden’s 1999 paper [2] summarizes the history and semantics of the quasiquoteation mechanism found in both the Scheme family of languages and in Common Lisp. In the Lisp family, program code is represented in a uniform manner, using lists that contain either atomic data, such as symbols, strings, and numbers, or further lists. In Lisp parlance, these structures are referred to as “S-expressions”. Because S-expressions are simply ordinary data, it makes sense to quote them, yielding a structure that can easily be manipulated. Additionally, most Lisps have a quasiquoteation system, in which specially marked subexpressions of a quoteation are evaluated, with the result substituted into the quoteation. Unlike Quine’s quasiquoteation, the Lisp family of languages allow arbitrary expressions to be inserted into quasiquoteations.

Languages outside of the Lisp family have also used quasiquoteation to implement language extension. Because these languages’ syntaxes do not have the regular format of Lisp S-expressions. The Camlp4 system [6] provides quasiquoteation for the OCaml language, among other extensions. In Camlp4, quasiquoteations consist of arbitrary strings that are transformed by a *quoteation expander* to either a string representing valid concrete syntax or to an abstract syntax tree. These quoteations support antiquoteation, which invokes the parser to read an OCaml expression or pattern inside of the quoteation. Template Haskell’s quasiquoteations [9] work on similar principles. Both systems fully expand all quoteations at compile time, and both check that the generated code is well-typed.

The MetaML family of metaprogramming facilities [15], including MetaOCaml [17] and F# [14], implement a style of quoteation in which the type of quoted expressions is parameterized over the type that would be inhabited by the the quoted expression if it were reified. These features are intended for use in staged computation. In addition to representing the types of the quoted expressions, these staging annotations feature static scope, so a quoteation that contains a name contains the version of that name from the scope in which the quoteation was generated.

Scala quasiquoteations [13] are very much like Lisp quasiquoteations. While their syntax resembles that of strings, this is a consequence of their implementation using Scala’s string interpolators and they are in fact expanded to ASTs at compile time. The quasiquoteations were initially intended to serve as an implementation technique for Scala macros [4], but they are also useful for both runtime code generation as well as generating program text. Scala macros closely resemble Lisp macros, in that they do not intend to allow arbitrary strings to be used as syntax, but instead implement transformations from one valid parse tree to another. Unlike Lisp, Scala programs that contain macros are type checked after macro expansion, and they are represented by a conventional AST that macros manipulate. Quasiquoteations are a means of constructing and destructuring these trees using the syntax of the high-level Scala language.

Like Scala, C# is an object-oriented language with a notion of quoteation [11]. In C#, quoteation can be applied to an anonymous function by annotating it with the `Expression` type, which causes

a datatype representing the function’s AST to be generated instead of the function itself. However, this feature cannot properly be considered quasiquoteation, as there is no mechanism for escaping the quoteation and inserting a sub-tree that has been generated elsewhere.

### 2.2 Reflection, Proof Automation, and Tactic Languages

The ML language was originally developed as a metalanguage for the Edinburgh LCF proof assistant [8]. In fact, this is where the name ML is derived from. An abstract datatype was used to represent rules of inference in the underlying logic, and ML functions could then be used to construct these proofs. Higher-order functions could then be used to represent strategies for combining these functions. ML served as an expressive language for automating the construction of proofs.

Agda [16] has a notion of *reflection*, described by van der Walt and Swierstra. Agda reflection is a form a compile-time metaprogramming, where quoted terms are used to construct proof terms that are then reified and type checked at compile time. These terms are constructed through direct manipulation of the term AST, which is a simple untyped lambda calculus. Agda metaprograms can get access to reflected representations of the type that is expected at a particular source location as well as its lexical environment, and they can then use this information to construct a term matching the expected type. However, users of reflection in Agda must program with a notation matching the reflected term datatype, rather than with ordinary Agda syntax.

Coq is perhaps the best-known system that is designed to facilitate automating the construction of proofs. Early versions of Coq required that users extend the built-in collection of tactics using OCaml. LTac [7] is a domain-specific language for writing new tactics that works at a higher level of abstraction than OCaml. It provides facilities for pattern matching the syntax of arbitrary terms from Coq’s term language Gallina, without these terms having been reduced to applications of constructors. Likewise, it can instantiate lower-level tactics and tacticals, which may contain Gallina terms, using portions of syntax extracted from the matched goals. Thus, LTac pattern matching can be considered a form of quasiquoteation.

More recently, Ziliani et al. developed the MTac tactic language [19]. Like Agda’s reflection mechanism and unlike LTac, MTac is implemented in Coq’s term language, rather than being an external language. However, unlike Agda’s reflection, MTac tactics use Coq’s type system to classify the terms produced by tactics, and the type system can therefore catch errors in tactics. Due to the elimination restrictions and impredicativity of the `Prop` universe, one can pattern match over the structure of arbitrary terms in MTac, rather than just terms in canonical form. MTac required only minimal extensions to Coq, namely a primitive to run MTac tactics.

## 3. Reflection in Idris

Idris’s reflection system is very similar to that of Agda. Elements of a datatype representing terms in a lambda calculus can be generated from the compiler’s internal representation of `TT`, after which Idris programs can manipulate them or use them as input to procedures that generate new reflected terms. In addition to generating new terms, Idris allows the generation of tactic scripts through reflection, by providing a collection of base tactics as a datatype along with a primitive tactic that allows functions from an environment and a goal to a reflected tactic to be used as tactics themselves. Naturally, the tactic that applies an Idris function as a tactic is itself reflected.

Unlike Agda, the terms that are available through Idris’s reflection mechanism are fully annotated with their types. Additionally, they include features of a development calculus in the style of McBride’s OLEG [10], including special binding forms for holes

and guesses. This representation is more complicated and more accurate than Agda’s, as it maintains typing information.

## 4. Idris Quasiquotations

TT is a minimalist dependently-typed  $\lambda$ -calculus with inductive-recursive families of types and operators defined by pattern matching. The full details of TT are available in Brady’s 2013 article [3].

Our quasiquotations extend the Idris<sup>-</sup> language, which is a version of Idris in which purely syntactic transformations such as the translation of do-notation and idiom brackets to their underlying functions have been performed and user-defined syntax extensions have been expanded. We extend the expression language with three new productions:

$$e, t ::= \dots$$

‘( e )	(quasiquotation of e)
‘( e : t )	(quasiquotation of e with type t)
~ e	(antiquotation of e)

The parts of a term between a quotation but not within an antiquotation are said to be *quoted*. Antiquotations that are not quoted, and quoted quasiquotations, are static errors. The quoted regions of a term are elaborated in the same way as any other Idris expression. However, instead of being used directly, the elaborated TT terms are first reflected. Non-quoted regions are elaborated directly into reflected terms, which are inserted as usual.

Names occurring in the quoted portion of a term do not obey the typical lexical scoping rules of names in Idris. This is because quoted terms are intended to be used in places other than where they are constructed, and their reification site may have completely different bindings for the same names. Therefore, all names in the quoted portion are taken to refer to the global scope. Because antiquotations are ordinary terms, they obey the ordinary scoping rules of the language.

Idris supports type-driven disambiguation of overloaded names. This feature is used for everything from literal syntax for number- and list-like structures to providing consistent naming across related libraries. This is also used to allow “punning” between some types and their constructors. For instance, `()` represents both the unit type and its constructor in Idris, and `(Int, String)` can represent either a pair type or a pair of types. In ordinary Idris programs, all top-level definitions are required to have type annotations, so type information is available to aid in disambiguation. In quasiquoted terms, however, this information is not available. Thus, the second variant of quasiquotation above allows a goal type to be provided. Like quoted terms, it is elaborated in the global environment. Because the goal type does not occur in the final reflected term and simply exists as a shorthand to avoid explicitly annotating names, goal types may not contain antiquotations.

A particularly instructive example that demonstrates the need for goal types is the unit and product types. Following Haskell, Idris uses a “pun” on its notation for products. Both the unit type and its constructor are written `()`, and `(2, "two")` is an inhabitant of `(Int, String)`. Additionally, because a pair of types is a perfectly valid construct in a dependently-typed system, `(Int, String)` could represent either a pair of types or a pair type — respectively, a member of `(Type, Type)` or member of `Type`. In the context of a quasiquotation, defaulting rules would need to be used to disambiguate `()` and `(Int, String)`, and whichever version was not the default would become very difficult to use. The distinction between `‘( () : () )` and `‘( () : Type )`, however, is easy to see and easy to remember.

## 5. Elaboration

The Idris elaborator, described in detail in Brady’s 2013 paper [3], uses proof tactics to translate desugared Idris to the core type theory

TT. A full presentation of this process is far outside the scope of this paper; however, enough details are repeated to make the elaboration of quasiquotes understandable.

### 5.1 The Elaboration Monad

The Idris elaborator is built on top of a library for manipulating terms in type theory. The elaborator is defined inside of a monad with state that consists of a hole queue, a focused hole or guess, and a collection of unsolved unification problems. The hole queue contains goals that are yet to be solved - at the beginning of elaboration, it will contain a single hole, but later operations can introduce new holes. The focused hole represents the current goal. Additionally, the elaboration monad contains errors and error handling.

A number of meta-operations, or *tactics*, are defined in the elaboration monad. These tactics resemble the built-in proof tactics of a system like Coq. In this paper, we use the following subset of Brady’s [3] meta-operations:

- CHECK, which type checks a complete term;
- CLAIM, which introduces a new hole with a particular type, placing it at the rear of the hole queue;
- GET, which binds the proof state to a variable;
- FILL, which adds a guess for the focused hole, solving the imposed unification constraints;
- NEWPROOF, which obliterates the proof state and establishes a new goal;
- PUT, which replaces the proof state with a new one;
- SOLVE, which causes a guess to be substituted for its hole;
- TERM, which returns the current term;
- UNFOCUS, which moves the focused hole to the end of the hole queue;

As a notational convention, we follow Brady [3] in letting the notation for names in the meta-language and names in the object language coincide, deferring to the reader to see which is being used. Names that occur in both contexts are metalanguage names referring to coinciding object language names. Additionally, unbound variables are taken to be fresh. When operations and their arguments occur under an arrow (e.g. CLAIM  $\vec{a}$ ), it means that the operation is repeated on all the arguments in the sequence. This is similar to `mapM` in Haskell.

The meta-operations  $\mathcal{E}[\cdot]$  and  $\mathcal{P}[\cdot]$ , which run relative to a proof state, respectively elaborate expressions and patterns. These operations usually coincide; however, they treat unresolved free variables differently. Following  $\mathcal{E}[\cdot]$ , unresolved holes or variables trigger an error, while unresolved names in patterns (that is, following  $\mathcal{P}[\cdot]$ ) are bound to pattern variables. Otherwise, constructors with implicit arguments (such as the length argument to the `(: :)` case of `Vect`) would not be able to be pattern-matched.

Elaboration is type-directed, in the sense that the elaborator always has a goal type available and can make decisions based on this fact. However, sometimes the type will be either unknown or partially known. In these cases, unification constraints imposed by the elaboration of the term can cause the type to be solved.

In addition to the meta-operations described by Brady [3], we define four additional operations:

- ANYTHING, which introduces a hole whose type must be inferred;
- EXTRACTANTIQUOTES, which replaces antiquotations in a quasiquoted Idris<sup>-</sup> term with references to fresh names, returning the modified term and the mapping from these fresh names to their corresponding antiquotation terms;

- REFLECT, which returns a term corresponding to the reflection of its argument; and
- REFLECTP, which returns a pattern corresponding to the reflection of its argument.

The operation ANYTHING  $n$  can be defined as follows:

$$\text{ANYTHING } n = \underline{\text{do}} \text{ CLAIM } (n' : \text{Type}) \\ \text{CLAIM } (n : n')$$

This represents type inference because it hides the fresh name  $n'$  that is introduced for the type of  $n$ . Thus, the type must be later solved through unification with other elaborated terms. EXTRACTANTIQUOTES is a straightforward traversal of an Idris<sup>-</sup> term, replacing antiquotations with variables and accumulating a mapping from these fresh variables to the corresponding replaced subterms. The names alone are accessed by the operation *names*. REFLECT and REFLECTP each take a term and a collection of names of antiquotations (see Section 5.2) and return a quoted version of the term. Antiquotation names, however, are not quoted. Additionally, REFLECTP inserts universal patterns in certain cases — see Section 5.4

## 5.2 Elaborating Quasiquotations

We implement quasiquotations by extending the elaboration procedures for expressions and patterns, respectively  $\mathcal{E}[\cdot]$  and  $\mathcal{P}[\cdot]$ . Elaborating the quoted term proceeds through five steps, each of which is described in detail below:

1. Replace all antiquotations by fresh variables, keeping track of the antiquoted terms and their assigned names
2. Elaborate the resulting term in a fresh proof state, to avoid variable capture
3. If RHS, quote the term, leaving antiquotation variables free
4. If LHS, quote with strategically placed universal patterns for things like unused names
5. Restore local environment and elaborate antiquotations

**Replace antiquotations** We replace antiquotations with fresh variables because they will need to be treated differently than the rest of the term. Additionally, the expected types of the antiquotations must be inferable from the context in which they are found, because the quotations that will fill them provide no type information. We remember the association between the antiquoted terms and the names that they were replaced by so that the result of elaborating them can later be inserted.

**Elaborate in a fresh proof state** Quotations can occur in any Idris expression. However, names that are defined in quotations are resolved in the global scope, for reasons discussed in Section 4. Because the scopes of local variables are propagated using hole contexts in the proof state, it is sufficient to elaborate the quoted term in a fresh state. The replacement of antiquotations with references to fresh names means that there is no risk of elaborating the contents of the antiquotations too early. However, when the elaborator reaches these names, it will fail, because they are unknown. To fix this problem, we first use the ANYTHING meta-operation that was defined above to introduce holes for both these names and their types. Because this stage of elaboration occurs in term mode, rather than pattern mode, the elaboration will fail if the holes containing types don't get solved through unification.

**Quote the term** Quotation is the first step that differs between terms and patterns. In both cases, the term resulting from elaboration is quoted, with the names that were assigned to antiquotations left unquoted. However, if the term being elaborated is a pattern,

$$\mathcal{E}[\langle e \rangle] = \underline{\text{do}} (e', \vec{a}) \leftarrow \text{EXTRACTANTIQUOTES } e \quad (1)$$

$$st \leftarrow \text{GET} \quad (2)$$

NEWPROOF  $T$

CLAIM ( $T : \text{Type}$ )

ANYTHING (*names*  $\vec{a}$ )

$\mathcal{E}[e']$

$qt \leftarrow \text{TERM}$

CHECK  $qt$

PUT  $st$

$$\text{CLAIM } (\textit{names } \vec{a} : \text{Term}) \quad (3)$$

$r \leftarrow \text{REFLECT } qt \vec{a}$

FILL  $r$

SOLVE

$$\text{ELABANTIQUOTE } \vec{a} \quad (5)$$

Figure 1. Elaboration of quasiquotations

then some aspects of the term are not quoted faithfully. See Section 5.4 for more information.

**Elaborate the antiquotations** The quoted term from the previous step is ready to be spliced into the original hole. What remains is to solve the variables introduced for antiquotations in the previous step. This is done by first introducing each name as a hole expecting a quoted term, and then elaborating them straightforwardly into their respective holes.

Figure 1 describes this elaboration procedure in Brady's notation. The individual tactics that correspond to each of the steps 1–5 above are numbered. Antiquotations are replaced in the first line of the tactic script, using the previously-described operation EXTRACTANTIQUOTES (1). Then, the ordinary state monad operations GET and PUT are used to save and restore the original proof state. The region (2) bracketed by these operations corresponds to step 2 above — namely, elaboration of the quoted term in the global context, which is achieved using a fresh proof state introduced by NEWPROOF. Initially, the goal of the new proof is an unbound variable, but this variable is then bound as a hole expecting a type using the CLAIM meta-operation. The quoted term is provided with hole bindings for each of the fresh antiquotation names by the ANYTHING meta-operation. Then, the quoted term is elaborated into the main hole. If this process is successful, it will result in the hole  $T$  being filled out with a concrete type as well. The result of elaboration is saved in the variable  $qt$ , and then type checked one final time with CHECK to ensure that no errors occurred.

After the original proof state is restored with PUT, the actual quoting must be performed and the antiquotations must be spliced into the result (3). Each antiquotation name is now established as a hole of type Term, the datatype representing reflected terms, because the elaborated form must be a quotation. Now that the holes for the antiquotations are established, it is possible to insert the reflected term into the initial hole. The operation REFLECT is invoked, which quotes the term, leaving references to the antiquotation variables intact as references to the just-introduce holes. This quoted term is then filled in as a guess, and SOLVE is used to dispatch the proof obligation.

Finally, the antiquotations can be elaborated (5). This is done by focusing on their holes and elaborating the corresponding term into that hole. In the above script, this is represented by the tactic ELABANTIQUOTE, which can be defined as follows:

$$\text{ELABANTIQUOTE } (n, t) = \underline{\text{do}} \text{ FOCUS } n \\ \mathcal{E}[t]$$

$$\mathcal{E}[\langle e : t \rangle] = \underline{\text{do}}$$

$$\begin{array}{l} \vdots \\ \text{CLAIM } (T : \text{Type}) \\ \text{FOCUS } T \\ \mathcal{E}[t] \\ \text{ANYTHING } (\vec{\text{names}} \vec{a}) \\ \vdots \end{array}$$

**Figure 2.** Elaborating quasiquotations with goal types

A specific elaboration procedure for antiquotations is not necessary, because programs with antiquotations outside of quasiquotations are rejected prior to elaboration.

### 5.3 Elaborating Goal Types

Elaborating a quasiquotation with an explicit goal type is a straightforward extension of the procedure in the previous section. After introducing a hole for the type of the term that will be elaborated prior to the actual quotation, the goal type is elaborated into this hole. Because this is occurring immediately after the establishment of a fresh proof state, names in the goal type will be resolved in the global scope, as intended.

The formal procedure is largely identical, with only the small addition shown in Figure 2. Thus, the lines immediately before and immediately after are included to show where the additions have occurred. This seemingly-simple change has far-reaching effects, because type information is now available to the subsequent elaboration of  $e'$ . This type information can, for instance, enable implicit arguments to be solved due to unification constraints induced by the elaboration of  $t$ .

### 5.4 Elaborating Quasiquotation Patterns

Quasiquotations can also be used as patterns. Recall that the operation  $\mathcal{P}[\cdot]$  is a variation of  $\mathcal{E}[\cdot]$  that is used on the left-hand side of definitions in order to elaborate patterns. The primary difference is that  $\mathcal{P}[\cdot]$  does not fail when the elaborated term contains unknown variables. Instead, it inserts pattern variable bindings for these.

It is tempting, then, to simply use the pattern elaborator in the recursive elaboration clauses of the quasiquote elaboration procedures. However, this would not work. REFLECT would simply quote these new pattern variables, leading to terms that contain explicitly quoted fresh pattern variables. Pattern elaboration must instead invoke ordinary expression elaboration when generating the term to be quoted, but then use pattern elaboration for the antiquotations.

For practical reasons, pattern elaboration must use a specialized reflection procedure REFLECTP that introduces some universal patterns in strategic places. For example, ordinary non-dependent function types are represented in TT as dependent functions in which the bound name is not free in the type on the right hand side. These names are chosen by the compiler, and they are difficult to predict. Therefore, they are represented as universal patterns ( $\_$ ) rather than their names. Additionally, universe level variables and internal type and constructor tag values are replaced with universal patterns. There is no solid theoretical basis for the current selection of universal pattern addition heuristics. Rather, it is a result of experimentation with the system and writing practical programs.

Figure 3 demonstrates the formal procedure for elaboration of quasiquotation patterns. This procedure uses two variations on previously-seen meta-operations: REFLECTP, like REFLECT, is a traversal of the resulting tree structure that implements step 4 above, and ELABANTIQUOTEP is defined as follows:

$$\mathcal{P}[\langle e \rangle] = \underline{\text{do}} (e', \vec{a}) \leftarrow \text{EXTRACTANTIQUOTES } e \quad (1)$$

$$st \leftarrow \text{GET} \quad (2)$$

$$\text{NEWPROOF } T$$

$$\text{CLAIM } (T : \text{Type})$$

$$\text{ANYTHING } (\vec{\text{names}} \vec{a})$$

$$\mathcal{E}[e']$$

$$qt \leftarrow \text{TERM}$$

$$\text{CHECK } qt$$

$$\text{PUT } st$$

$$\text{CLAIM } (\vec{\text{names}} \vec{a} : \vec{\text{Term}}) \quad (4)$$

$$r \leftarrow \text{REFLECTP } qt \vec{a}$$

$$\text{FILL } r$$

$$\text{SOLVE}$$

$$\text{ELABANTIQUOTEP } \vec{a} \quad (5)$$

**Figure 3.** Elaborating quasiquote patterns

$$\text{ELABANTIQUOTEP } (n, t) = \underline{\text{do}} \text{FOCUS } n$$

$$\mathcal{P}[t]$$

The modifications necessary to elaborate a quasiquotation pattern with a goal type are identical to the non-pattern case. In the real implementation, of course, quasiquote elaboration with or without goal types and in pattern mode or expression mode is handled by one code path, with conditionals expressing the four possibilities. They are presented as four separate procedures here for reasons of clarity.

## 6. Examples

This section demonstrates the usefulness of quasiquotations through a number of examples, showing how the high-level notation of Idris quasiquotation simplifies their expression and reduces the need for the user to comprehend all of the details of elaboration.

### 6.1 Custom Tactics

In Idris, a custom tactic is a function from a proof context and goal to a reflected tactic expression. Reflected tactics are represented by the `Tactic` datatype, which has constructors such as `Exact` for solving the goal with some proof term, `Refine` for applying a name to solve the goal, leaving holes for the remaining arguments, and `Skip` which does nothing, along with tactics such as `Seq` for sequential composition and `Try` to provide a fallback in case of errors. These tactics correspond to the elaborator tactics described in Section 5.

The native tactic `applyTactic` runs a custom tactic in the scope of the current proof. In other words, its argument should be an expression of type:

```
List (TTName, Binder TT) -> TT -> Tactic
```

This construction allows Idris to be its own metalanguage for purposes of proof automation.

#### 6.1.1 Trivial Goals

When writing proofs, it may be the case that a particular goal is completely trivial. Either the goal type is one such as  $()$  or the equality type that have only a single constructor, or we have a premise available with precisely the type that we desire. Idris already has a built-in tactic to solve these kinds of goals, called `trivial`. However, this built-in tactic is not extensible with support for new trivial types.

Figure 4 demonstrates an implementation of a trivial tactic that uses our newly-introduced quasiquotations. The first case checks

```

triv : List (TTName, Binder TT) -> TT -> Tactic
triv ctxt '(() : Type) =
  Exact '(() : ())
triv ctxt '((=) {A=~A} {B=~B} ~x ~y) =
  Exact '(the ((=) {A=~A} {B=~B} ~x ~y) refl)
triv ((n, b)::ctxt) goal =
  if binderTy b == goal
  then Exact (P Bound n Erased)
  else triv ctxt goal
triv [] _ =
  Fail [TextPart "Decidedly nontrivial!"]

```

Figure 4. A tactic for trivial goals

```

rewrite_plusSuccRightSucc : TT -> Maybe Tactic
rewrite_plusSuccRightSucc '(plus ~n (S ~m)) =
  Just (Rewrite '(plusSuccRightSucc ~n ~m))
rewrite_plusSuccRightSucc _ = Nothing

rewrite_plusZeroRightNeutral : TT -> Maybe Tactic
rewrite_plusZeroRightNeutral '(plus ~n Z) =
  Just (Rewrite '(sym (plusZeroRightNeutral ~n)))
rewrite_plusZeroRightNeutral _ = Nothing

```

Figure 5. Rewriters for addition

whether the goal is the unit type. The goal annotation is necessary because of Idris’s defaulting rules, which prioritize the unit constructor during disambiguation. The second case checks whether the goal is an identity type. The explicit provision of both A and B is necessary because Idris uses heterogeneous equality, and the elaborator is unable to guess what these types are. The third case provides for a traversal of the context, checking whether a proof is already available. Finally, the fourth case causes an error to be thrown if the proof was not trivial.

### 6.1.2 Simplifying Arithmetic Expressions

The function `plus` that implements natural number addition is defined by recursion on its first argument. This means that certain equalities that users may consider to be trivial, such as  $n + Succ(m) = Succ(n + m)$ , exist as lemmas in the library that must be explicitly applied. This process is entirely tedious and can be automated. However, a general-purpose search mechanism that attempted to use the entire standard library to rewrite equalities to something easily provable would very likely be too slow and fragile to use. This is an excellent use for a custom tactic.

Indeed, a family of such tactics can be defined using a simple combinator language. In this example, we define rewriters for arithmetic expressions involving addition, zero, and successors, but the approach can easily be extended to cover more equalities.

Let a *rewriter* be a function in `TT -> Maybe Tactic`. A rewriter, when passed a goal, should either return a tactic that simplifies the goal or `Nothing`. Figure 5 demonstrates two rewriters for addition. The first uses the library proof `plusSuccRightSucc`, which expresses the identity  $n + Succ(m) = Succ(n + m)$ . The second uses the proof `plusZeroRightNeutral`, which expresses that zero is a right-identity of addition. Quasiquotes provide a convenient notation for both pattern-matching the goal terms and constructing the proof objects to rewrite with. Without quasiquotes, the first example would be much longer, as can be seen in Figure 6.

It is important to point out that this is a particularly *easy* case to translate. The function is monomorphic, with no implicit arguments to be solved. The types in question are first-order, with no pa-

```

rewrite_plusSuccRightSucc : TT -> Maybe Tactic
rewrite_plusSuccRightSucc
  (App
    (App
      (P Ref (NS (UN "plus") ["Nat", "Prelude"]) _)
      n)
    (App
      (P (DCon 1 _)
        (NS (UN "S") ["Nat", "Prelude"])
        _))
    m)) =
  Just (Rewrite
    (App (App (P Ref
      (NS (UN "plusSuccRightSucc")
        ["Nat", "Prelude"])
      _)
      n)
    m))
rewrite_plusSuccRightSucc _ = Nothing

```

Figure 6. A rewriter, without quasiquotes

rameters or indices. In many realistic programs, especially those in which implicit arguments must be solved, the relationship between the term to be rewritten and its low-level reflected representation might be much more difficult to discern.

Returning to the rewriting library, we can define a few simple combinators:

```

(<||>) : (TT -> Maybe Tactic) ->
  (TT -> Maybe Tactic) ->
  TT -> Maybe Tactic
rewrite_eq : (TT -> Maybe Tactic) ->
  TT -> Maybe Tactic
rewrite_nat : (TT -> Maybe Tactic) ->
  TT -> Maybe Tactic

```

The `<||>` operator attempts to rewrite using its left-hand rewriter. If this fails, it will attempt to rewrite with its right-hand operator. The operators `rewrite_eq` and `rewrite_nat` recurse over the structure of the goal, attempting to apply rewrite rules at each step. They apply to equality types and natural number expressions, respectively.

It is possible to derive a rewriter for equalities of expressions involving natural numbers and addition as follows:

```

rewrite_eq
  (rewrite_nat
    (rewrite_plusSuccRightSucc <||>
      rewrite_plusZeroRightNeutral))

```

This rewriter can be used in a custom tactic to repeatedly rewrite until a normal form has been reached.

## 6.2 Error Reflection

As described in the introduction and in a previous paper [5], Idris’s *error reflection* allows programmatic rewriting of error messages. This can be used to provide domain-specific errors for embedded domain-specific languages, but most type errors are of the form “Can’t unify  $t_1$  with  $t_2$ ”, where  $t_1$  and  $t_2$  can be arbitrarily large terms. Additionally, dependent types often lead to a lot of redundant information being retained on terms in order to propagate type information - and much of this information is collected on implicit arguments that need to be inferred by the elaborator anyway. Without quasiquotation, pattern-matching on these terms inside of reflected error messages is extremely verbose and error-prone.

```

%error_handler
vectRewrite : Err -> Maybe (List ErrorReportPart)
vectRewrite (CantUnify x
             '(Vect ~n ~a)
             '(Vect ~m ~b)
             _ _ _) =
  if n /= m
  then Just [TextPart "Mismatching lengths."]
  else Nothing
vectRewrite _ = Nothing

```

**Figure 7.** Error rewriter for vector lengths

As a simple example, Figure 7 demonstrates an error message rewriter provides a hint to users who attempt to use a vector whose length does not match the expected length. This code will cause unification errors between two vector types, when their lengths are not identical, to be replaced by the message “Mismatching lengths”. For reasons of space, this is a very simple example. The equivalent of just one of the patterns, `'(Vect ~n ~a)`, is:

```

App (App (P (TCon _ 2)
           (NS (UN "Vect") ["Vect", "Prelude"]))
     (Bind _
          (Pi (P (TCon _ 0)
                (NS (UN "Nat")
                    ["Nat", "Prelude"]))
              Erased))
      (Bind _
           (Pi (TType _)
                (TType _))))
    n)
a

```

where the universal patterns are a result of the special quoting rules that are applied in a pattern context.

This example was very simple. Many realistic error rewriting rules are much more complicated. Without quasiquotes, the error reflection feature would be worthless, because the effort required to manually elaborate terms would be far too great.

## 7. Conclusion and Future Work

This paper introduced a quasiquotation feature in the Idris language. These quotations can decrease the verbosity of reflection and allow the use of the implicit argument resolution mechanisms and type-driven overloading when constructing reflected terms. Idris’s type-driven elaboration mechanism [3] needed only a small amount of new code in order to handle this unforeseen extension, providing evidence that the approach can scale to new features.

The present implementation of quasiquotation has one major limitation: the elaboration of some terms in the high-level Idris language results in auxiliary definitions, which are then referenced in the elaborated `TT` terms. This is because, in `TT`, all pattern matching must occur at the top level. As an example, `case` blocks and pattern-matching `lets` are elaborated into top-level functions. Presently, the quotations of these terms simply refer to names of definitions that do not exist. Potential solutions to this problem include rejecting terms with this kind of side effect or tracking the original syntax that results in auxiliary definitions, so that two quotations of the same high-level term will refer to the same auxiliary name. Neither potential solution is entirely satisfactory.

Presently, the elaboration of quasiquote patterns introduces a number of universal patterns in invisible parts of the term where the user would not be able to predict or control the contents, such as machine-generated unused names. However, the locations at

which these patterns are inserted is currently not well founded in experience, and it may match too many terms. It would be useful to have a means of being more precise, or possibly even using dependent pattern matching to ensure a kind of restricted  $\alpha$ -equivalence between the term being destructured and the quoted term in the pattern.

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